

*- Neutrosophic Crisp Set & *- Neutrosophic Crisp relations

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Abstract. Since the world is full of indeterminacy, the neutrosophics found their place into contemporary research. The purpose of this paper is to introduce a new type of neutrosophic crisp set as the *- neutrosophic crisp sets as a generalization to star intuitionistic set due to Indira et al.[4], and study some of

its properties. Finally we introduce and study the notion of \ast -neutrosophic relation and some of its properties.

Keywords: Neutrosophic Crisp Set; Star Intuitionistic Sets; Neutrosophic Relations; Neutrosophic Data.

1 Introduction

The fundamental concepts of neutrosophic set, introduced by Smarandache in [31, 32, 33], and Salama et al. in [5, 6, 7, 8, 9, 10, 11, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30], provides a natural foundation for treating mathematically the neutrosophic phenomena which exist pervasively in our real world and for building new branches of neutrosophic mathematics. Neutrosophy has laid the foundation for a whole family of new mathematical theories generalizing both their classical and fuzzy counterparts [1, 2, 12, 22, 34] such as a neutrosophic set theory. In this paper we introduce a new type of neutrosophic crisp set as the *- neutrosophic crisp set, and study some of its properties. Finally we introduce and study the notion of *- neutrosophic relation and some of its properties. Possible applications to mathematical computer are touched upon.

2 Terminologies

We recollect some relevant basic preliminaries, and in particular, the work of Smarandache in [31, 32, 33], and Salama et al. in [5, 6, 7, 8, 9, 10, 11, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30]. Smarandache introduced the neutrosophic components T, I, F which represent the membership, indeterminacy, and non-membership values respectively, where 0.01^{+} is nonstandard unit interval.

3 *- Neutrosophic Crisp Sets

We shall now consider some possible definitions for a new type of neutrosophic crisp set

Definition 3.1

Let *X* be a non-empty fixed set. A neutrosophic crisp set (NCS for short) *A* is an object having the form $A = \langle A_1, A_2, A_3 \rangle$.

Then we define the *- neutrosophic set A^* as $A^* = \langle A_1 \cap (A_2 \cup A_3)^c, A_2 \cap (A_1 \cup A_3)^c, A_3 \cap (A_1 \cup A_2)^c \rangle$ where A_1, A_2 and A_3 are subsets of X such that $M = A_1 \cap (A_2 \cup A_3)^c$, $S = A_2 \cap (A_1 \cup A_3)^c$ and $R = A_3 \cap (A_1 \cup A_2)^c$.

A *- neutrosophic crisp set is an object having the form $A^* = \langle M, S, R \rangle$

Lemma 3.1

Let X be a non-empty fixed sample space. A neutro-sophic crisp set (NCS for short) A is an object having the form $A = \langle A_1, A_2, A_3 \rangle$. Then

$$A^* = \left\langle A_1 \cap (A_2 \cup A_3)^c, A_2 \cap (A_1 \cup A_3)^c, A_3 \cap (A_1 \cup A_2)^c \right\rangle \text{ is also a neutrosophic crisp set.}$$

Proof

It's clear.

Corollary 3.1

Let *X* be a non-empty fixed set. Then ϕ_N^* and X_N^* are also neutrosophic crisp set.

Theorem 3.1

Let X be a non-empty fixed sample space, two neutrosophic crisp sets A, B are having the form

$$A = \langle A_1, A_2, A_3 \rangle$$
, $B = \langle B_1, B_2, B_3 \rangle$, and two *- neutrosophic sets $A^* = \langle M_1, S_1, R_1 \rangle$, $B^* = \langle M_2, S_2, R_3 \rangle$ where $M_1 = A_1 \cap (A_2 \cup A_3)$, $S_1 = A_2 \cap (A_1 \cup A_3)^c$,

$$R_1 = A_3 \cap (A_1 \cup A_2)^c$$
, $M_2 = B_1 \cap (B_2 \cup B_3)^c$,
 $S_2 = B_2 \cap (B_1 \cup B_3)^c$, and
 $R_2 = B_3 \cap (B_1 \cup B_2)$, Then $A \subseteq B$ implies $A^* \subseteq B^*$.

Proof

Given $A \subseteq B$. Then it is easy to prove that $M_1 \subseteq M_2$, $S_1 \subseteq S_2, R_1 \supseteq R_2$ or $M_1 \subseteq M_2$, $S_1 \subseteq S_2, R_1 \supseteq R_2$ So $A^* \subset B^*$

Remark 3.1

- 1) All types of ϕ_N^* and ϕ_N are concedes.
- 2) All types of X_N^* and X_N are concedes.
- 3) $A^* = B^* \text{ iff } A^* \subseteq B^* \text{ and } B^* \subseteq A^*$.

Definition 3.8

Let X be a non-empty set, and $A^* = \langle M, S, R \rangle$ be a *-neutrosophic crisp set on a NCS $A = \langle A_1, A_2, A_3 \rangle$ where $M = A_1 \cap (A_2 \cup A_3)^c$, $S = A_2 \cap (A_1 \cup A_3)^c$, $R = A_3 \cap (A_1 \cup A_2)^c$, Then the complement of the set A^* (A^{*c} , for short) may be defined as three kinds of complements

$$(C_1)$$
 Type1: $A^{*c} = \langle M^c, S^c, R^c \rangle$,

$$(C_2)$$
 Type2: $A^{*^c} = \langle R, S, M \rangle$,

$$(C_3)$$
 Type3: $A^{*c} = \langle R, S^c, M \rangle$.

Definition 2.3

Let X be a non-empty fixed set, two neutrosophic crisp sets A, B are having the form $A = \langle A_1, A_2, A_3 \rangle$,

 $B = \langle B_1, B_2, B_3 \rangle$, and two *- neutrosophic crisp

sets
$$A^* = \langle M_1, S_1, R_1 \rangle, B^* = \langle M_2, S_2, R_2 \rangle$$
 where

$$M_1 = A_1 \cap (A_2 \cup A_3)^c$$
, $S_1 = A_2 \cap (A_1 \cup A_3)^c$,

$$R_1 = A_3 \cap (A_1 \cup A_2)^c$$
, $M_2 = B_1 \cap (B_2 \cup B_3)^c$,

 $S_2 = B_2 \cap (B_1 \cup B_3)^c$, and

$$R_2 = B_3 \cap (B_1 \cup B_2)^c$$
, Then

1) $A^* \cap B^*$ may be defined as two types: i) Type1: $A^* \cap B^* = \langle M_1 \cap M_1, S_2 \cap S_2, R_3 \cup R_3 \rangle$ or

i. Type2:
$$A^* \cap B^* = \langle M_1 \cap M_1, S_2 \cup S_2, R_3 \cup R_3 \rangle$$

4) $A^* \cup B^*$ may be defined as two types:

i) Type1:
$$A^* \cup B^* = \langle M_1 \cup M_1, S_2 \cap S_2, R_3 \cap R_3 \rangle$$
 or

ii) Type2:
$$A^* \cup B^* = \langle M_1 \cup M_1, S_2 \cup S_2, R_3 \cap R_3 \rangle$$
.

Lemma 3.1

Let A^*, B^* are *- neutrosophic crisp sets. Then $A^* - B^* = A^* \cap B^{*^C}$

It easy to show that L. H. S is also a *- neutrosophic crisp sets.

Example 3.2

Let
$$X = \{a,b,c,d,e,f\}$$
, $A = \langle \{a,b,c,d\}, \{e\}, \{f\} \rangle$,

$$B = \langle \{a,b,c\}, \{d\}, \{e\} \rangle, C = \langle \{a,b\}, \{c,d\}, \{e,f,a\} \rangle$$

$$D = \langle \{a,b\}, \{e,c\}, \{f,d\} \rangle$$
 are NCS. Then

$$A^* = \langle \{a, b, c, d\}, \{e\}, \{f\} \rangle, B^* = \langle \{a, b, c\}, \{d\}, \{e\} \rangle,$$

$$C^* = \langle \{b\}, \{c,d\}, \{e,f\} \rangle$$

The complement may be equal as:

$$A^{*c} = \langle \{e, f\}, \{a, b, c, d, f\}, \{a, b, c, d\} \rangle,$$

$$A^{*c} = \langle \{ \{ f \}, \{ e \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A^{*c} = \langle \{ \{ f \}, \{ a, b, c, d \}, \{ a, b, c, d \} \rangle, A$$

$$2)C^{*c} = \langle \{a, c, d, f\}, \{a, b, e, f\}, \{a, b, c, d\} \rangle,$$

$$C^{*c} = \langle \{e, f\}, \{c, d\}, \{b\} \rangle, C^{*c} = \langle \{e, f\}, \{a, b, e, f\}, \{b\} \rangle.$$

 $3)A^* \cup B^*$ may be equals the following forms

$$A^* \cup B^* = \langle \{a, b, c, d\}, \{e\}, \phi \rangle,$$

$$A^* \cup B^* = \langle \{a,b,c,d\}, \phi, \{f\} \rangle,$$

 $4)A^* \cap B^*$ may be equals the following forms

$$A^* \cap B^* = \langle \{a, b, c\}, \{e, d\}, \{f, e\} \rangle,$$

$$A^* \cup B^* = \langle \{a, b, c\}, \phi, \{f, e\} \rangle,$$

Proposition 3.1

Let $\{A_j^*: j \in J\}$ be arbitrary family of *- neutrosophic crisp subsets on X, then

- 1) $\bigcap A_i^*$ may be defined two types as:
 - i) Type1: $\bigcap A^*_j = \langle \bigcap M_j, \bigcap S_j, \bigcup R_j \rangle$, or
 - ii) Type2: $\bigcap A^*_j = \langle \bigcap M_j, \bigcup S_j, \bigcup R_j \rangle$.
- 2) $\cup A^*_i$ may be defined two types as :

i) Type1:
$$\bigcup A_j^* = \langle \bigcup M_i, \bigcap S_i, \bigcap R_i \rangle$$
 or

ii) Type2:
$$\bigcup A^*_{j} = \langle \bigcup M_{j}, \bigcup S_{j}, \bigcap R_{j} \rangle$$
.

Corollary 3.2

Let $\{A_i\}$ be a NCSs in X where $i \in J$, where J is an index set and $\{A_i^*\}$ are corresponding *- neutrosophic crisp subsets on X then

- a) $A_i^* \subset B^*$ for each $i \in J \Rightarrow \bigcup A_i^* \subset B^*$.
- b) $B^* \subset A_i^*$ for each $i \in J \Rightarrow B^* \subset \cup A_i^*$.
- c) $(\bigcup A_i^*)^c = \bigcap A_i^{*c} : (\bigcap A_i^*)^c = \bigcup A_i^{*c}$.

- d) $A_i^* \subseteq B^* \Leftrightarrow B^{*^c} \subseteq A^{*^c}$.
- e) $A^{*c}^{c} = A$,
- f) $\phi_N^{*^c} = X_N; X_N^{*^c} = \phi_N^*.$

Now we shall define the image and preimage of *-neutrosophic crisp set.

Let X,Y be two non-empty fixed sets and $f:X\to Y$, be a function and $A=\langle A_1,A_2,A_3\rangle$, $B=\langle B_1,B_2,B_3\rangle$ are neutrosophic crisp sets on X and Y respectively, $A^*=\langle M_1,S_1,R_1\rangle$, $B^*=\langle M_2,S_2,R_2\rangle$ be the *- neutrosophic crisp sets on X and Y respectively.

Definition 3.9

- (a) If B^* is a *- NCS in Y, then the preimage of B^* under f, denoted by $f^{-1}(B^*)$, is a *- NCS in X defined by $f^{-1}(B^*) = \left\langle f^{-1}(M_2), f^{-1}(S_2), f^{-1}(R_2) \right\rangle$
- (b) If A^* is a *- NCS in X, then the image of A^* under f, denoted by $f(A^*)$, is the *- NCS in Y defined by $f(A^*) = \langle f(M_1), f(S_1), f(R_1)^c \rangle \rangle$.

Here we introduce the properties of images and preimages some of which we shall frequently use in the following.

Corollary 3.2

Let A^* , $\left\{A_i^*: i \in J\right\}$, be a family of *- NCS in X, and B^* , $\left\{B_j^*: j \in K\right\}$ *- NCS in Y, and $f: X \to Y$ a function. Then

(a) $A_1^* \subseteq A_2^* \Leftrightarrow f(A_1^*) \subseteq f(A_2^*)$,

$$B_{1}^{*} \subseteq B_{2}^{*} \Leftrightarrow f^{-1}(B_{1}^{*}) \subseteq f^{-1}(B_{2}^{*}),$$

- (b) $A^* \subseteq f^{-1}(f(A^*))$ and if f is injective, then $A^* = f^{-1}(f(A^*))$,
- (c) $f^{-1}(f(B^*)) \subseteq B^*$ and if f is surjective, then $f^{-1}(f(B^*)) = B^*$,
- (d) $f^{-1}(\cup B_i^*) = f^{-1}(B_i^*), f^{-1}(\cap B_i^*) = \cap f^{-1}(B_i^*),$
- (e) $f(\cup A_{ii}^*) = \cup f(A_{ii}^*)$; $f(\cap A_{ii}^*) \subseteq \cap f(A_{ii}^*)$; and if f is injective, then $f(\cap A_{ii}^*) = \cap f(A_{ii}^*)$;
- (f) $f^{-1}(Y^*_N) = X^*_N$, $f^{-1}(\phi^*_N) = \phi^*_N$.
- (g) $f(\phi^*_N) = \phi^*_N$, $f(X^*_N) = Y^*_N$, if f is surjective.
- (h) If f is surjective, then $(f(A^*))^c \subseteq f(A^*)^c$. if furthermore f is injective, then have $(f(A^*))^c = f(A^*)^c$.
- (i) $(f^{-1}(B^*)^c = (f^{-1}(B^*))^c$.

Proof

Clear by definitions.

4 *- Neutrosophic Crisp Set Relations

Here we give the definition relation on *- neutrosophic crisp sets and study of its properties.

Let X, Y and Z be three ordinary nonempty sets

Definition 4.1

Let X be a non-empty fixed set, two neutrosophic crisp sets $A \cdot B$ are having the form $A = \langle A_1, A_2, A_3 \rangle$,

 $B = \langle B_1, B_2, B_3 \rangle$, and two *- neutrosophic crisp

sets $A^* = \langle M_1, S_1, R_1 \rangle, B^* = \langle M_2, S_2, R_2 \rangle$ where

 $M_1 = A_1 \cap (A_2 \cup A_3), \quad S_1 = A_2 \cap (A_1 \cup A_3),$

 $R_1 = A_3 \cap (A_1 \cup A_2),$

 $M_2 = B_1 \cap (B_2 \cup B_3), S_2 = B_2 \cap (B_1 \cup B_3), \text{ and}$

 $R_2 = B_3 \cap (B_1 \cup B_2)$, Then

i) The product of two *- neutrosophic crisp sets A^* and B^* is a *- neutrosophic crisp set $A^* \times B^*$ given by $A^* \times B^* = \langle M_1 \times M_2, S_1 \times S_2, R_1 \times R_2 \rangle$ on $X \times Y$.

ii) We will call a *- neutrosophic crisp relation $R^* \subseteq A^* \times B^*$ on the direct product $X \times Y$.

The collection of all *- neutrosophic crisp relations on $X \times Y$ is denoted as $SNCR(X \times Y)$

Definition 4.2

Let R^* be a *- neutrosophic crisp relation on $X \times Y$, then the inverse of R^* is donated by R^{*-1} where $R^* \subset A^* \times B^*$ on $X \times Y$ then $R^{*-1} \subset B^* \times A^*$ on $Y \times X$.

Example 4.1

Let $X = \{a, b, c, d, e, f\}$, $A = \langle \{a, b, c, d\}, \{e\}, \{f\} \rangle$,

 $B = \langle \{a, b, c\}, \{d\}, \{e\} \rangle$, are NCS.

the product of two *- neutrosophic crisp sets given by

 $A^* \times B^* = \left\langle \{(a,a),(a,b),(a,c),(b,a),(b,b),(b,c),(c,a),(c,b),(c,c)\},\{(e,d)\},\{(f,e)\}\right\rangle$ and

 $B^* \times A^* = \left\{ \{(a,a),(a,b),(a,c),(a,d),(b,a),(b,b),(b,c),(b,d),(c,a),(c,b),(c,c),(c,d) \}, \{(d,e)\}, \{(e,f)\} \right\}$

, and $R_1^* = \langle \{(a,a)\}, \{(c,c)\}, \{(d,d)\} \rangle, R_1^* \subseteq A^* \times B^*$ on $X \times X$,

 $R_2^* = \langle \{(a,b)\}, \{(c,c)\}, \{(d,d),(b,d)\} \rangle R_2^* \subseteq B^* \times A^* \text{ on }$

 $X \times X$, $R_1^{*-1} = \langle \{(a,a)\}, \{(c,c)\}, \{(d,d)\} \rangle \subset B^* \times A^*$ and

 $R_2^{*-1} = \langle \{(b,a)\}, \{(c,c)\}, \{(d,d),(d,b)\} \rangle \subseteq B^* \times A^*.$

We can define the operations of *- neutrosophic crisp relations.

Definition 4.3

Let R^* and S^* be two *- neutrosophic crisp relations between X and Y for every $(x, y) \in X \times Y$ and NCSS A and B in the form $A = \langle A_1, A_2, A_3 \rangle$, A^* on X,

 $B = \langle B_1, B_2, B_3 \rangle$, B^* on Y Then we can defined the following operations

- i) $R \subset S$ may be defined as two types
- a) Type1: $R^* \subseteq S^* \Leftrightarrow M_{1_p} \subseteq M_{1_s}$, $S_{1_p} \subseteq S_{1_s}$,

 $R_{1_n} \supseteq R_{1_n}$

b) Type2:

$$R^* \subseteq S^* \iff M_{1_R} \subseteq M_{1_S}, S_{1_R} \supseteq S_{1_S}, R_{1_R} \supseteq R_{1_S}$$

- ii) $R^* \cup S^*$ may be defined as two types
- a) Type1:

$$R^* \cup S^* = \langle M_{1R} \cup M_{1S}, S_{1R} \cup S_{1S}, R_{1R} \cap R_{1S} \rangle$$

b) Type2:

$$R^* \cup S^* = \langle M_{1R} \cup M_{1S}, S_{1R} \cap S_{1S}, R_{1R} \cap R_{1S} \rangle.$$

- iii) $R^* \cap S^*$ may be defined as two types
- a) Type1:

$$R^* \cap S^* = \langle M_{1R} \cap M_{1S}, S_{1R} \cup S_{1S}, R_{1R} \cup R_{1S} \rangle,$$

b) Type2:

$$R^* \cap S^* = \langle M_{1R} \cap M_{1S}, S_{1R} \cap S_{1S}, R_{1R} \cup R_{1S} \rangle$$
.

Theorem 4.1

Let R^* , S^* and Q^* be three *- neutrosophic crisp relations between X and Y for every $(x, y) \in X \times Y$, then

i)
$$R^* \subseteq S^* \Rightarrow R^{*-1} \subseteq S^{*-1}$$

ii)
$$\left(R^* \cup S^*\right)^{-1} \Rightarrow R^{*-1} \cup S^{*-1}$$

iii)
$$\left(R^* \cap S^*\right)^{-1} \Rightarrow R^{*-1} \cap S^{*-1}$$
.

iv)
$$\left(R^{*-1}\right)^{-1} = R^*$$
.

v)
$$R^* \cap (S^* \cup Q^*) = (R^* \cap S^*) \cup (R^* \cap Q^*).$$

vi)
$$R^* \cup (S^* \cap Q^*) = (R^* \cup S^*) \cap (R^* \cup Q^*)$$
.

vii) If $S^* \subset R^*$, $O^* \subset R^*$, then $S^* \cup O^* \subset R^*$.

Proof

Clear

Definition 5.4

The *- neutrosophic crisp relation $I^* \in SNCR^*(X \times X)$, the *- neutrosophic crisp relation of identity may be defined as two types

i) Type1:
$$I^* = \left\{ \left\{ \left\{ A^* \times A^* \right\}, \left\{ A^* \times A^* \right\}, \phi^* > \right\} \right\}$$

ii) Type2:
$$I^* = \{ \{A^* \times A^*\}, \phi^*, \phi^* > \}$$

Now we define two composite relations of *- neutro-sophic crisp sets.

Definition 5.5

Let R^* be a *- neutrosophic crisp relation in $X \times Y$, and S^* be a neutrosophic crisp relation in $Y \times Z$. Then the

composition of R^* and S^* , $R^* \circ S^*$ be a *- neutrosophic crisp relation in $X \times Z$ as a definition may be defined as two types

i) Type1:

$$R^* \circ S^* \leftrightarrow (R^* \circ S^*)(x,z)$$

$$= \cup \{ \langle \{(M_1 \times M_2)_R \cap (M_1 \times M_2)_S \},$$

$$\{(S_1 \times S_2)_R \cap (S_1 \times S_2)_S\}, \{(R_1 \times R_2)_R \cap (R_1 \times R_2)_S\} > .$$

ii) Type2:

$$R^* \circ S^* \longleftrightarrow (R^* \circ S^*)(x,z)$$

$$= \cap \{ \langle \{(M_1 \times M_2)_R \cup (M_1 \times M_2)_S \},$$

$$\{(S_1 \times S_2)_R \cup (S_1 \times S_2)_S\}, \{(R_1 \times R_2)_R \cup (R_1 \times R_2)_S\} > .$$

Theorem 4.2

Let R^* be a *- neutrosophic crisp relation in $X \times Y$, and S be a *- neutrosophic crisp relation in $Y \times Z$ then $(R^* \circ S^*)^{-1} = S^{*-1} \circ R^{*-1}$.

Proo

Let $R^* \subset A^* \times B^*$ on $X \times Y$ then $R^{*-1} \subset B \times A$,

 $S^* \subseteq B^* \times D^*$ on $Y \times Z$ then $S^{*-1} \subseteq D^* \times B^*$, from Definition 4.3 and similarly we

can
$$I^*_{(R^* \circ S^*)^{-1}}(x, z) = I^*_{S^{*-1}}(x, z)$$
 and $I^*_{R^{*-1}}(x, z)$ then
$$(R^* \circ S^*)^{-1} = S^{*-1} \circ R^{*-1}$$

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