# FLORENTIN SMARANDACHE Conjectures On Primes' Summation 

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## CONJECTURES ON PRIMES' SUMMATION

A) Any odd integer $n$ can be expressed as a combination of three primes as follows:

1) As a sum of two primes minus another prime:
$\mathrm{n}=\mathrm{p}+\mathrm{q}-\mathrm{r}$, where $\mathrm{p}, \mathrm{q}, \mathrm{r}$ are all prime numbers.
Do not include the trivial solution: $p=p+q-q$ when $p, q$ are prime.
For example: $1=3+5-7=5+7-11=7+11-17=11+13-23=\ldots$;
$3=5+5-7=7+19-23=17+23-37=\ldots ;$
$5=3+13-11=\ldots$;
$7=11+13-17=\ldots$;
$9=5+7-3=\ldots$;
$11=7+17-13=$ ...
a) Is this conjecture equivalent to Goldbach's Conjecture (any odd integer $>=9$ is the sum of three primes)?
b) Is the conjecture true when all three prime numbers are different?
c) In how many ways can each odd integer be expressed as above?
2) As a prime minus another prime and minus again another prime:
$\mathrm{n}=\mathrm{p}-\mathrm{q}-\mathrm{r}$, where $\mathrm{p}, \mathrm{q}, \mathrm{r}$ are all prime numbers.
For example: $1=13-5-7=17-5-11=19-5-13=\ldots$;

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3=13-3-7=23-7-13=\ldots ;
$$

$$
5=13-3-5=\ldots ;
$$

$$
7=17-3-7=.
$$

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\ldots
$$

$$
9=17-3-5=\ldots
$$

$$
11=19-3-5=\ldots .
$$

a) Is this conjecture equivalent to Goldbach's Conjecture ?
b)Is the conjecture true when all three prime numbers are different?
c) In how many ways can each odd integer be expressed as above?
B) Any dd integer an can he cunreced as a onmhination of five primes as follows:
3) $n=p+q \div r+t-u$, where $p, q, r, t, u$ are all prime numbers, and $\mathrm{t} \neq \mathrm{u}$.
For example: $1=3+3+3+5-13-3+5+5+17-29-\ldots$;

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$$
\begin{aligned}
& 3=3+5+11+13-29=\ldots ; \\
& 5=3+7+11+13-29=\ldots ; \\
& 7=5+7+11+13-29=\ldots ; \\
& 9=5+7+11+13-29=\ldots ; \\
& 11=5+7+11+17-29=\ldots
\end{aligned}
$$

a) Is the conjecture true when all five prime numbers are different"?
b) In how many ways can each odd integer be expressed as above"?
4) $n=p+q+r-t-u$, where $p, q, r, t, u$ are all prime numbers, and $t, u \neq p$, q, r.
For example: $1=3+7+17-13-13=3+7+23-13-19=$

$$
\begin{aligned}
& 3=5+7+17-13-13=\ldots ; \\
& 5=7+7+17-13-13=\ldots ; \\
& 7=5+11+17-13-13=\ldots ; \\
& 9=7+11+17-13-13=\ldots ; \\
& 11=7+11+19-13-13=\ldots
\end{aligned}
$$

a) Is the conjecture true when all five prime numbers are different?
b) In how many ways can each odd integer be expressed as above?
5) $n=p+q-r-t-u$, where $p, q, r, t, u$ are all prime numbers, and $r, t, u \neq p, q$. For example: $1=11+13-3-3-17=\ldots$;

$$
\begin{aligned}
& 3=13+13-3-3-17=\ldots ; \\
& 5=3+29-5-5-17=\ldots ; \\
& 7=3+31-5-5-17=\ldots ; \\
& 9=3+37-7-7-17=\ldots ; \\
& 11=5+37-7-7-17=\ldots
\end{aligned}
$$

a) Is the conjecture true when all five prime numbers are different?
b) In how many ways can each odd integer be expressed as above?
6) $n=p-q-r-t-u$, where $p, q, r, t . u$ are all prime numbers, and $q . r . t . u \neq p$. For example: $1=13-3-3-3-3=\ldots$;

$$
\begin{aligned}
& 3=17-3-3-3-5=\ldots ; \\
& 5=19-3-3-3-5=\ldots ; \\
& 7=23-3-3-5-5=\ldots ; \\
& 9=29-3-5-5-7=\ldots ; \\
& 11=31-3-5-5-7=\ldots .
\end{aligned}
$$

a) Is the conjecture true when all five prime numbers are different?

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b) In how many ways can each odd integer be expressed as above?

## GENERAL CONJECTURI:

Let $k \geq 3$, and $\mathrm{l}<\mathrm{s}<\mathrm{k}$, be integers. Then:
i) If $k$ is odd, any odd integer can be expressed as a sum of $k$-s primes (first set) minus a sum of sprimes (second set)
[such that the primes of the first set is different from the primes of the second set].
a) Is the conjecture true when all k prime numbers are different?
b) In how many ways can each odd integer be expressed as above?
ii) If $k$ is even, any even integer can be expressed as a sum of $k$-s primes (first set) minus a sum of $s$ primes (second set)
[such that the primes of the first set is different from the primes of the second set].
a) Is the conjecture true when all k prime numbers are different?
b) In how many ways can each even integer be expressed as above?

Reference:
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