

Case Retrieval in Medical Databases by Fusing Heterogeneous Information

Gwénoél Quéléc*, Mathieu Lamard, Guy Cazuguel, *Member, IEEE*, Christian Roux, *Fellow, IEEE*, and Béatrice Cochener

Abstract—A novel content-based heterogeneous information retrieval framework, particularly well suited to browse medical databases and support new generation computer aided diagnosis (CADx) systems, is presented in this paper. It was designed to retrieve possibly incomplete documents, consisting of several images and semantic information, from a database; more complex data types such as videos can also be included in the framework. The proposed retrieval method relies on image processing, in order to characterize each individual image in a document by their digital content, and information fusion. Once the available images in a query document are characterized, a degree of match, between the query document and each reference document stored in the database, is defined for each attribute (an image feature or a metadata). A Bayesian network is used to recover missing information if need be. Finally, two novel information fusion methods are proposed to combine these degrees of match, in order to rank the reference documents by decreasing relevance for the query. In the first method, the degrees of match are fused by the Bayesian network itself. In the second method, they are fused by the Dezert-Smarandache theory: the second approach lets us model our confidence in each source of information (i.e., each attribute) and take it into account in the fusion process for a better retrieval performance. The proposed methods were applied to two heterogeneous medical databases, a diabetic retinopathy database and a mammography screening database, for computer aided diagnosis. Precisions at five of 0.809 ± 0.158 and 0.821 ± 0.177 , respectively, were obtained for these two databases, which is very promising.

Index Terms—Diabetic retinopathy, heterogeneous information retrieval, information fusion, mammography, medical databases.

Manuscript received June 15, 2010; revised July 26, 2010; accepted July 26, 2010. Date of publication August 05, 2010; date of current version December 30, 2010. Asterisk indicates corresponding author.

*G. Quéléc is with the Department of Image et Traitement de l'Information (ITI), Institut Telecom/Telecom Bretagne, F-29200 Brest, France, and also with the Institut National de la Santé et de la Recherche Médicale (INSERM) U650, F-29200 Brest, France (e-mail: gwenole.quelec@telecom-bretagne.eu).

G. Cazuguel and C. Roux are with the Department of Image et Traitement de l'Information (ITI), Institut Telecom/Telecom Bretagne, F-29200 Brest, France, and also with the Institut National de la Santé et de la Recherche Médicale (INSERM) U650, F-29200 Brest, France (e-mail: guy.cazuguel@telecom-bretagne.eu; christian.roux@telecom-bretagne.eu).

M. Lamard is with the University of Bretagne Occidentale, Brest, F-29200, France, and also with the Institut National de la Santé et de la Recherche Médicale (INSERM) U650, F-29200 Brest, France (e-mail: mathieu.lamard@univ-brest.fr).

B. Cochener is with the Centre Hospitalier Universitaire de Brest, Service d'Ophthalmologie, F-29200 Brest, France, and with the University of Bretagne Occidentale, F-29200 Brest, France, and also with the Institut National de la Santé et de la Recherche Médicale (INSERM) U650, F-29200 Brest, France (e-mail: beatrice.cochener-lamard@chu-brest.fr).

Color versions of one or more of the figures in this paper are available online at <http://ieeexplore.ieee.org>.

Digital Object Identifier 10.1109/TMI.2010.2063711

I. INTRODUCTION

TWO main tasks in computer aided diagnosis (CADx) using medical images are extraction of relevant information from images and combination of the extracted features with other sources of information to automatically or semi-automatically generate a reliable diagnosis. One promising way to achieve the second goal is to take advantage of the growing number of digital medical databases either for heterogeneous data mining, i.e., for extracting new knowledge, or for heterogeneous information retrieval, i.e., for finding similar heterogeneous medical records (e.g., consisting of digital images and metadata). This paper presents a generic solution to use digital medical databases for heterogeneous information retrieval, and solve CADx problems using case-based reasoning (CBR) [1].

CBR was introduced in the early 1980s as a new decision support tool. It relies on the idea that analogous problems have similar solutions. In CBR, interpreting a new situation revolves around the retrieval of relevant documents in a case database. The knowledge of medical experts is a mixture of textbook knowledge and experience through real life clinical cases, so the assumption that analogous problems have similar solutions makes sense to them. This is the reason why there is a growing interest in CBR for the development of medical decision support systems [2]. Medical CBR systems are intended to be used as follows: should a physician be doubtful about his/her diagnosis, he/she can send the available data about the patient to the system; the system selects and displays the most similar documents, along with their associated medical interpretations, which may help him/her confirm or invalidate his/her diagnosis by analogy. Therefore, the purpose of such a system is not to replace physicians' diagnosis, but rather to aid their diagnosis. Medical documents often consist of digital information such as images and symbolic information such as clinical annotations. In the case of diabetic retinopathy, for instance, physicians analyze heterogeneous series of images together with contextual information such as the age, sex and medical history of the patient. Moreover, medical information is sometimes incomplete and uncertain, two problems that require a particular attention. As a consequence, original CBR systems, designed to process simple documents such as homogeneous and comprehensive attribute vectors, are clearly unsuited to complex CADx applications. On one hand, some CBR systems have been designed to manage symbolic information [3]. On the other hand, some others, based on content-based image

retrieval [4], have been designed to manage digital images [5]. However, few attempts have been made to merge the two kinds of approaches. We consider in this paper a larger class of problems: CBR in heterogeneous databases.

To retrieve heterogeneous information, some simple approaches, based on early fusion (i.e., attributes are fused in feature space) [6], [7] or late fusion (i.e., attributes are fused in semantic space) [8]–[10] have been presented in the literature. A few application-specific approaches [11]–[15], as well as a generic retrieval system, based on dissimilarity spaces and relevance feedback [16], have also been presented. We introduce in this paper a novel generic approach that does not require relevance feedback from the user. The proposed system is able to manage incomplete information and the aggregation of heterogeneous attributes: symbolic and multidimensional digital information (we focus on digital images, but the same principle can be applied to any n -dimensional signals). The proposed approach is based on a Bayesian network and the Dezert–Smarandache theory (DSmT) [17]. Bayesian networks have been used previously in retrieval systems, either for keyword based retrieval [18], [19] or for content-based image or video retrieval [20], [21]. The Dezert–Smarandache theory is more and more widely used in remote sensing applications [17], however, to our knowledge, this is its first medical application. In our approach, a Bayesian network is used to model the relationships between the different attributes (the extracted features of each digital image and each contextual information field): we associate each attribute with a variable in the Bayesian network. It lets us compare incomplete documents: the Bayesian network is used to estimate the probability of unknown variables (associated with missing attributes) knowing the value of other variables (associated with available attributes). Information coming from each attribute is then used to derive an estimation of the degree of match between a query document and a reference document in the database. Then, these estimations are fused; two fusion operators are introduced in this paper for this purpose. The first fusion operator is incorporated in the Bayesian network: the computation of the degree of match, with respect to a given attribute, relies on the design of conditional probabilities relating this attribute to the overall degree of match. An evolution of this fusion operator that models our confidence in each source of information (i.e., each attribute) is introduced. It is based on the Dezert–Smarandache theory. In order to model our confidence in each source of information, within this second fusion operator, an uncertainty component is included in the belief mass function characterizing the evidence coming from this source of information.

The main advantage of the proposed approach, over standard feature selection/feature classification approaches, is that a retrieval model is trained separately for each attribute. This is useful to process incomplete documents: in the proposed approach, we simply combine the models associated with all available attributes; as a comparison, a standard classifier relies on feature combinations, and therefore may become invalid when input feature vectors are incomplete. Also, because each attribute is processed separately, the curse of dimensionality is avoided. Therefore, it is not necessary to select the most relevant features: instead, we simply weight each feature by a confidence measure.

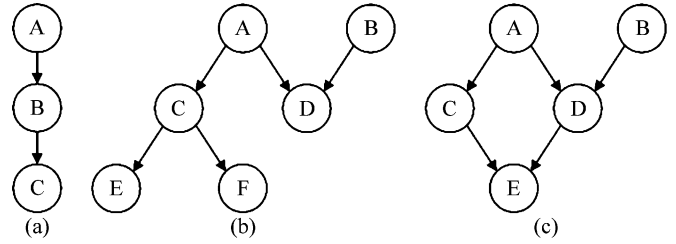


Fig. 1. Examples of Bayesian networks. (a) A chain. (b) A polytree, i.e., a network in which there is at most one (undirected) path between two nodes. (c) A network containing a cycle: $\langle A, D, E, C, A \rangle$.

The paper is organized as follows. Section II presents the proposed Bayesian network based retrieval. Section III presents the Bayesian network and Dezert–Smarandache theory based retrieval. These methods are applied in Section IV to CADx in two heterogeneous databases: a diabetic retinopathy database and a mammography database. We end with a discussion and a conclusion in Section V.

II. BAYESIAN NETWORK BASED RETRIEVAL

A. Description of Bayesian Networks

A Bayesian network [22] is a probabilistic graphical model that represents a set of variables and their probabilistic dependencies. It is a directed acyclic graph whose nodes represent variables, and whose edges encode conditional independencies between the variables. Examples of Bayesian networks are given in Fig. 1.

In the example of Fig. 1(b), the edge from the parent node A to its child node D indicates that variable A has a direct influence on variable D . Each edge in the graph is associated with a conditional probability matrix expressing the probability of a child variable given one of its parent variables. For instance, if $A = \{a_0, a_1\}$ and $D = \{d_0, d_1, d_2\}$, then $A \rightarrow D$ is assigned the following (3×2) conditional probability matrix $P(D|A)$

$$P(D|A) = \begin{pmatrix} P(D = d_0|A = a_0) & P(D = d_0|A = a_1) \\ P(D = d_1|A = a_0) & P(D = d_1|A = a_1) \\ P(D = d_2|A = a_0) & P(D = d_2|A = a_1) \end{pmatrix}. \quad (1)$$

A directed acyclic graph is a Bayesian Network relative to a set of variables $\{X_1, \dots, X_n\}$ if the joint distribution $P(X_1, \dots, X_n)$ can be expressed as in

$$P(X_1, \dots, X_n) = \prod_{i=1}^n P(X_i | \text{parents}(X_i)) \quad (2)$$

where $\text{parents}(X)$ is the set of nodes such that $Y \rightarrow X$ is in the graph $\forall Y \in \text{parents}(X)$. Because a Bayesian network can completely model the variables and their relationships, it can be used to answer queries about them. Typically, it is used to estimate unknown probabilities for a subset of variables when other variables (the evidence variables) are observed. This process of computing the posterior distribution of variables, given evidence, is called probabilistic inference. In Bayesian networks

containing cycles, exact inference is a NP-hard problem. Approximate inference algorithms have been proposed, but their accuracies depend on the network's structure; therefore, they are not general. By transforming the network into a cycle-free hypergraph, and performing inference in this hypergraph, Lauritzen and Spiegelhalter proposed an exact inference algorithm with relatively low complexity [23]; this algorithm was used in the proposed system.

B. Learning a Bayesian Network From Data

A Bayesian network is defined by a structure and the conditional probability of each node given its parents in that structure (or its prior probability if it does not have any parent). These parameters can be learned automatically from data. Defining the structure consists in finding pairs of nodes (X, Y) directly dependent, i.e., such that:

- X and Y are not independent ($P(X, Y) \neq P(X)P(Y)$);
- there is no node set \mathcal{Z} such that X and Y are independent given \mathcal{Z} ($P(X, Y|\mathcal{Z}) \neq P(X|\mathcal{Z})P(Y|\mathcal{Z})$).

Independence and conditional independence can be assessed by mutual information [see (3)] and conditional mutual information [see (4)], respectively

$$I(X, Y) = \sum_{x, y} P(x, y) \log \frac{P(x, y)}{P(x)P(y)} \quad (3)$$

$$I(X, Y|\mathcal{Z}) = \sum_{x, y, z} P(x, y, z) \log \frac{P(x, y|z)}{P(x|z)P(y|z)} \quad (4)$$

Two nodes are independent (resp. conditionally independent) if mutual information (resp. conditional mutual information) is smaller than a given threshold ϵ , $0 \leq \epsilon < 1$. Ideally, ϵ should be equal to 0. However, in the presence of noise, some meaningless edges (links) can appear. These edges can also unnecessarily increase the computation time. To avoid this, in this study, ϵ was chosen in advance to be equal to 0.1. This number is independent of dataset cardinality [24].

The structure of the Bayesian network, as well as edge orientation, was obtained by Cheng's algorithm [24]. This algorithm was chosen for its complexity: complexity is polynomial in the number of variables, as opposed to exponential in competing algorithms.

C. Including Images in a Bayesian Network

Contextual information are included as usual in a Bayesian network: a variable with a finite set of states, one for each possible attribute value, is defined for each field.

To include images in a Bayesian network, we first define a variable for each image in the sequence. For each "image variable," we follow the usual steps of Content-Based Image Retrieval (CBIR) [4]: 1) building a signature for each image (i.e., extracting a feature vector summarizing their digital content), and 2) defining a distance measure between two signatures (see Section II-C-1). Thus, measuring the distance between two images comes down to measuring the distance between two signatures. Similarly, in a Bayesian network, defining states for an "image variable" comes down to defining states for the signature of the corresponding images. To this aim, similar image signatures are clustered, as described below, and each cluster is

associated with a state. Thanks to this process, image signatures can be included in a Bayesian network like any other variable.

1) *Image Signature and Distance Measure:* In previous works on CBIR, we proposed to extract a signature for images from their wavelet transform [25]. These signatures model the distribution of the wavelet coefficients in each subband of the decomposition; as a consequence they provide a multiscale description of images. To characterize the wavelet coefficient distribution in a given subband, Wouwer's work was applied [26]: Wouwer has shown that this distribution can be modeled by a generalized Gaussian function. The maximum likelihood estimators of the wavelet coefficient distribution in each subband are used as a signature. These estimators can be computed directly from wavelet-based compressed images (such as JPEG-2000 compressed images), which can be useful when a large number of images has to be processed. A simplified version of Do's generalized Gaussian parameter estimation method [25], [27] is proposed in Appendix A to reduce computation times. Any wavelet basis can be used to decompose images. However, the effectiveness of the extracted signatures largely depends on the choice of this basis. For this reason, we proposed to search for an optimal wavelet basis [25] within the lifting scheme framework, which is implemented in the compression standards. To compare two signatures, Do proposed the use of the Kullback–Leibler divergence between wavelet coefficient distributions P and Q in two subbands [27]

$$D(P||Q) = \int_{\mathbb{R}} p(x) \log \frac{p(x)}{q(x)} dx \quad (5)$$

where p and q are the densities of P and Q , respectively. A symmetric version of the Kullback–Leibler divergence was used, since clustering algorithms require (symmetric) distance measures

$$\frac{1}{2} (D(P||Q) + D(Q||P)). \quad (6)$$

Finally, the distance between two images is defined as a weighted sum of these distances over the subbands, noted WSD ; weights are tuned by a genetic algorithm to maximize retrieval performance on the training set [25]. The ability to select a weight vector and a wavelet basis makes this image representation highly tunable. We have shown in previous works the superiority of the proposed image signature, in terms of retrieval performance, over several well-known image signatures [25].

2) *Signature Clustering:* In order to define several states for an "image variable," similar images are clustered with an unsupervised classification algorithm, thanks to the image signatures and the associated distance measure above. Any algorithm can be used, provided that the distance measure can be specified. We chose the well-known fuzzy C-means algorithm (FCM) [28] and replaced the Euclidean distance by WSD described above. In this algorithm, each document is assigned to each cluster $k = 1 \dots K$ with a fuzzy membership u_k , $0 \leq u_k \leq 1$, such that $\sum_{k=1}^K u_k = 1$, which can be interpreted as a probability. Finding the right number of clusters is generally a difficult problem. However, when each sample has been assigned a class label, mutual information between clusters and class labels can

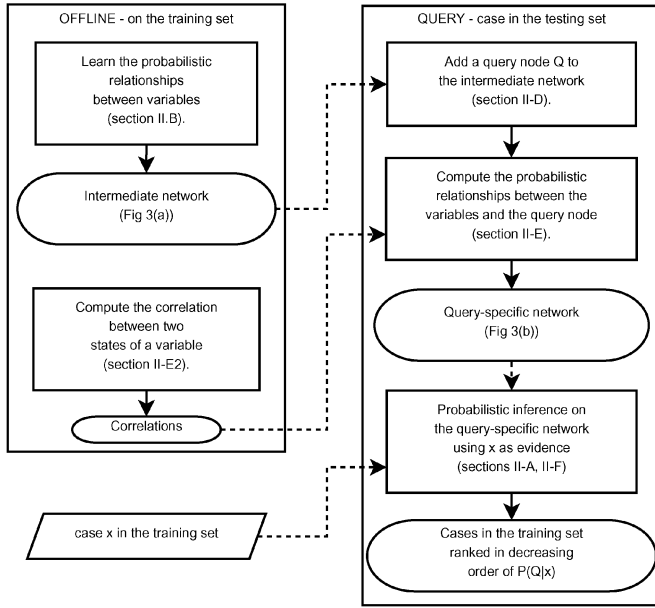


Fig. 2. Bayesian network based retrieval. Solid-lined arrows mean “leads to” or “is followed by” and dashed-lined arrows mean “is used by.”

be used to determine the optimal number of clusters \hat{K} [29] [see (7)]

$$\hat{K} = \arg \max_K \sum_{c=1}^C \sum_{k=1}^K P(c, k) \log_{C+K} \frac{P(c, k)}{P(c)P(k)} \quad (7)$$

where $c = 1 \dots C$ are the class labels, $P(c, k)$ is the joint probability distribution function of the class and cluster labels, $P(c)$ and $P(k)$ are the marginal probability distribution functions. Other continuous variables can be discretized similarly: the age of a person, 1-D signals, videos, etc.

D. System Design

Let x_q be a query document and M be the number of attributes.

Definition: A document x is said to be relevant for x_q if x and x_q belong to the same class.

To assess the relevance of each reference document in a database for x_q , we define a Bayesian network with the following variables:

- a set of variables $\{A_i, i = 1 \dots M\}$, where A_i represents the i th attribute of x ;
- a Boolean variable $Q = “x$ is relevant for $x_q”$ ($\bar{Q} = “x$ is not relevant for $x_q”$).

The design of the system is described hereafter and illustrated in Fig. 2. To build the network, the first step is to learn the different relationships between the attributes $\{A_i, i = 1 \dots M\}$. So, an intermediate network is built from data, using Cheng’s algorithm (see Section II-B). In that purpose, the studied database is divided into a training dataset and a test dataset. Cheng’s algorithm is applied to the training dataset. In our experiments, the query document x_q belongs to the test dataset and x belongs to the training dataset. To build this Bayesian network, a finite

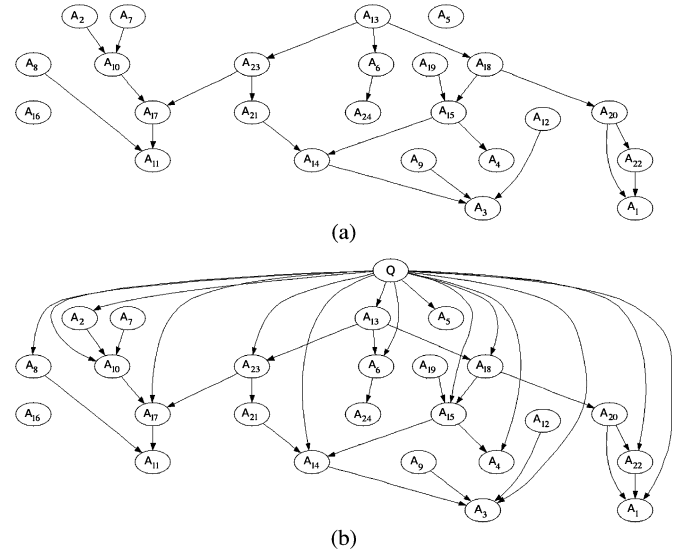


Fig. 3. Retrieval Bayesian Network (built for the database presented in Section IV-A). In the example of (b), attributes $A_1, \dots, A_6, A_8, A_{10}, A_{13}, A_{14}, A_{15}, A_{17}, A_{18}, A_{22}, A_{23}$ are available for the query document x_q , so the associated nodes are then connected to node Q . (a) Intermediate network. (b) Query-specific network.

number of states a_{ij} is defined for each variable $A_i, i = 1 \dots M$. To learn the relationships between these variables, we use the membership degree of any document y in the training dataset to each state a_{ij} of each variable A_i , noted $\alpha_{ij}(y)$. If A_i is a nominal variable, $\alpha_{ij}(y)$ is boolean; for instance, if y is a male then $\alpha_{\text{sex}, \text{male}}(y) = 1$, and $\alpha_{\text{sex}, \text{female}}(y) = 0$. If A_i is a continuous variable (such as an image-based feature), $\alpha_{ik}(y)$ is the fuzzy membership of y to each cluster $k = 1 \dots K$ (see Section II-C-2). An example of intermediate network is given in Fig. 3(a).

Q is then integrated in the network. For retrieval, the attributes of x are observable evidences for Q , as a consequence the associated variables should be descendants of Q . In the retrieval network, the probabilistic dependences between Q and each variable A_i depend on x_q . In fact, x_q specifies which attributes should be found in the retrieved documents in order to meet the user’s needs. So, when the i th attribute of x_q is available, we connect the two nodes Q and A_i and we estimate the associated conditional probability matrix $P_q(A_i = a_{ij}|Q)$ according to x_q [see Fig. 3(b)]. The index q denotes that the probability depends on x_q . A query-specific network is obtained: its structure depends on which attributes are available for the query document and the conditional probability matrices depend on the value taken for these available attributes by the query document. This network is used to assess the relevance of any reference document for x_q .

E. Computing the Conditional Probabilities $P_q(A_i = a_{ij}|Q)$

To compute $P_q(A_i = a_{ij}|Q)$, we first estimate $P_q(Q|A_i = a_{ij})$: the probability that a reference document x , with full membership to the state a_{ij} of attribute A_i , is relevant. $P_q(A_i = a_{ij}|Q)$ can then be computed thanks to Bayes’ theorem [see (8)]. The prior probability $P_q(Q)$ is required; it can be estimated by the probability that two documents belong to the same class,

i.e., the probability that both documents belong to class 1 or that both documents belong to class 2, etc., hence (9)

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)} \quad (8)$$

$$P_q(Q) = \sum_{c=1}^C (P(c))^2 \quad (9)$$

where $c = 1 \dots C$ are the class labels (as a consequence the prior probability $P_q(Q)$ is actually independent of x_q).

1) *Objectives:* We want to define $P_q(Q|A_i = a_{ij})$ such that the posterior probability $P_q(Q|x)$ is as close to 1 as possible if x and x_q belong to the same class, and as close to 0 as possible otherwise (note that the class label of x_q is unknown). We define the semantic similarity between documents x and x_q , with respect to A_i , as follows:

$$\sum_j \sum_k \alpha_{ij}(x) S_{ijk} \alpha_{ik}(x_q) \quad (10)$$

where S_{ikl} is the correlation between two states a_{ik} and a_{il} of A_i , regarding the class of the documents at these states.

2) *Correlation Between Two States of a Variable:* To compute S_{ikl} , we first compute the mean membership D_{ikc} (resp. D_{ilc}) of documents y in a given class c to the state a_{ik} (resp. a_{il}) (y belongs to the training dataset):

$$\begin{cases} D_{ijc} = \beta \frac{\sum_y \delta(y,c) \alpha_{ij}(y)}{\sum_y \delta(y,c)} \\ \sum_{c=1}^C (D_{ijc})^2 = 1, \quad \forall(i,j) \end{cases} \quad (11)$$

where $\delta(y,c) = 1$ if y is in class c , $\delta(y,c) = 0$ otherwise, and β is a normalizing factor chosen to meet the second relation. S_{ikl} is given by

$$S_{ikl} = \sum_{c=1}^C D_{ikc} D_{ilc}. \quad (12)$$

3) *Degree of Match Between x and x_q With Respect to A_i :* When computing the posterior probability $P_q(Q|x)$, the Bayesian inference algorithm fuses probabilities $P_q(Q|A_i)P(A_i)$ coming from each node A_i connected to Q [see Fig. 3(b)]. In the remainder of this paper, probability $dm_i(x, x_q) = P_q(Q|A_i)P(A_i)$ is referred to as the degree of match between x and x_q with respect to attribute A_i . This degree of match can be rewritten as follows:

$$dm_i(x, x_q) = \sum_j P_q(Q|A_i = a_{ij}) \alpha_{ij}(x) \quad (13)$$

where $\alpha_{ij}(x)$, the membership degree of x to the state a_{ij} of A_i , is known or computed by the Bayesian network. $P_q(Q|A_i = a_{ij})$ is chosen proportional to $r_{ij} = \sum_{k=1}^M \alpha_{ik}(x_q) S_{ijk}$. It implies that $dm_i(x, x_q)$ is proportional to the semantic similarity between x and x_q (13). As a consequence, the reference documents maximizing the semantic similarity with x_q will maximize $P_q(Q|x)$, which was our objective. Computation details for $P_q(Q|A_i = a_{ij})$ are given in Appendix B.

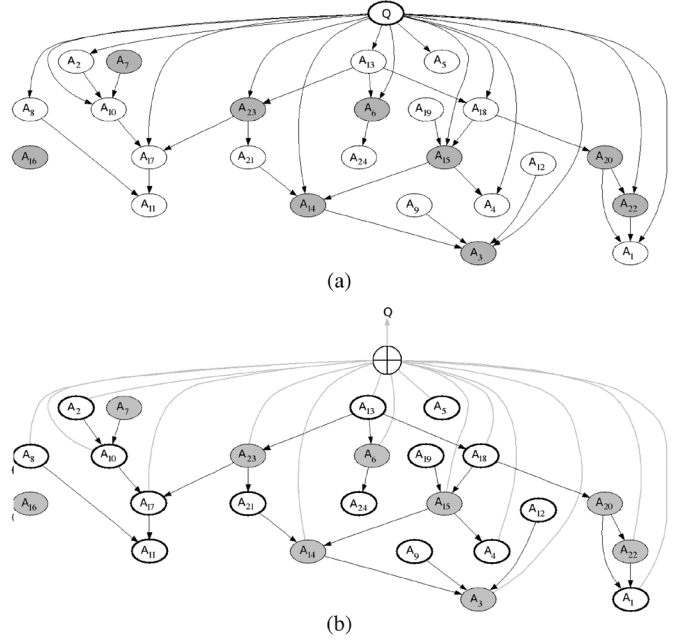


Fig. 4. Assessing the relevance of a reference document x for the query by the proposed methods. In this example, attributes $A_6, A_7, A_{14}, A_{15}, A_{16}, A_{20}, A_{22}$ and A_{23} are available for x_q . Evidence nodes are colored in gray and target nodes are brightly encircled. In (b), the fusion system is colored in gray (\oplus). (a) Bayesian network based method. (b) Bayesian network + DSMT based method.

F. Retrieval Process

The different reference documents in the database are then processed sequentially. To process a document x , every available attribute for x is processed as evidence and Lauritzen and Spiegelhalter's inference algorithm is used to compute the posterior probability of each variable, the posterior probability of Q , $P_q(Q|x)$, in particular [see Fig. 4(a)]. The reference documents in the database are then ranked in decreasing order of the computed posterior probability $P_q(Q|x)$.

III. BAYESIAN NETWORK AND DEZERT-SMARANDACHE BASED RETRIEVAL

A. Description of the Dezert-Smarandache Theory

The Dezert-Smarandache Theory (DSmT) of plausible and paradoxical reasoning, proposed in recent years [17], lets us combine any types of independent sources of information represented in term of belief functions. It generalizes the theory of belief functions (Dempster-Shafer Theory—DST) [30], which itself generalizes the Bayesian theory, used in the system above. DSmT is mainly focused on the fusion of uncertain, highly conflicting and imprecise sources of evidence.

Let $\theta = \{\theta_1, \theta_2, \dots\}$ be a set of hypotheses under consideration for the fusion problem; θ is called the frame of discernment. For our problem, $\theta = \{\bar{Q}, Q\}$. In Bayesian theory, a probability $P(\theta_i)$ is assigned to each element θ_i of the frame, such that $\sum_{\theta_i \in \theta} P(\theta_i) = 1$. More generally, in DST, a belief mass $m(A)$ is assigned to each element A of the power set $2^\theta = \{\emptyset, Q, \bar{Q}, Q \cup \bar{Q}\}$, i.e., the set of all composite propositions built from elements of θ with \cup operators, such that

$m(\emptyset) = 0$ and $\sum_{A \in 2^\theta} m(A) = 1$. Belief masses let us express our uncertainty; it is possible for instance to define confidence intervals on probabilities: depending on external circumstances, the probability of Q can range from $m(Q)$ and $m(Q) + m(Q \cup \bar{Q})$. DSMT takes one step further: a (generalized) belief mass $m(A)$ is assigned to each element A of the hyper-power set $D(\theta) = \{\emptyset, Q, \bar{Q}, Q \cap \bar{Q}, Q \cup \bar{Q}\}$, i.e., the set of all composite propositions built from elements of θ with \cap and \cup operators, such that $m(\emptyset) = 0$ and $\sum_{A \in D(\theta)} m(A) = 1$.

The belief mass functions m_i must be first specified by the user for each source of information, $i = 1 \dots M$ (m_i functions used in our system are described below, in Paragraph III-C). Then, mass functions m_i are fused into the global mass function m_f , according to a given rule of combination. Another difference between DST and DSMT comes from the underlying rules of combinations. Several rules, designed to better manage conflicts between sources, were proposed in DSMT, including the hybrid rule of combination [17] and the proportional conflict redistribution (PCR) rules [31]. It is possible to introduce constraints in the model [17]: we can specify pairs of incompatible hypotheses (θ_a, θ_b) , i.e., each subset A of $\theta_a \cap \theta_b$ must have a null mass, noted $A \in C(\theta)$.

Once the fused mass function m_f has been computed, we can compute the belief (credibility) and the plausibility of each hypothesis A (or any other element of $D(\theta)$) as follows:

$$Bel(A) = \sum_{B_i \subseteq A, B_i \in D(\theta)} m_f(B_i) \quad (14)$$

$$Pl(A) = \sum_{B_i \cap A \in C(\theta) \cup \emptyset, B_i \in D(\theta)} m_f(B_i) = 1 - Bel(\bar{A}). \quad (15)$$

Belief and plausibility are respectively pessimistic and optimistic. Pignistic probability [32], a possible compromise, is used instead (see below, in Paragraph III-D); other probabilistic transformations are available [33].

B. Link With Bayesian Network Based Retrieval

Our motivation for using the theory of belief functions, instead of the Bayesian theory, is that the former lets us model our confidence in each source of information, instead of taking each piece of information at face value. This property is particularly attractive for a medical decision support system where heterogeneous sources of information, with varying reliability, are combined. Because its fusion operators better manage conflicting sources of information, a common occurrence when these sources are unreliable, DSMT was used instead of the original theory of belief functions.

In the Bayesian network based method (see Section II), the relevance of a reference document for the query, according to a given attribute A_i , has been estimated through the design of conditional probabilities $P_q(Q|A_i = a_{ij})$. The M sources of information (represented by the network variables A_i , $i = 1 \dots M$) were then fused by the Bayesian network inference algorithm [see Fig. 3(b)] to compute the posterior probability of Q , $P_q(Q|x)$, for a document x in the database. We can translate this Bayesian fusion problem into the framework of the belief mass theory. Let $\theta = \{\bar{Q}, Q\}$ be the frame of

discernment. For each source $i(A_i)$, we defined (13) a degree of match $dm_i(x, x_q)$ between x and the query x_q , which may be viewed as the belief mass $m_i(Q)$ assigned to hypothesis Q and consequently $m_i(\bar{Q}) = 1 - m_i(Q)$ was assigned to \bar{Q} .

In that first approach, we did not model our confidence in the estimation of the relevance provided by each source of evidence (through the design of conditional probabilities). And poor estimations of the relevance provided by some sources might mislead the computation of the fused estimation. So we would like to give more importance in the fusion process to the trusted sources of evidence. We propose to use DSMT to model our confidence in each source of evidence, as explained below.

C. System Design

To extend the previous method in the DSMT framework, we assign a mass not only to Q and \bar{Q} , but to each element in $D(\theta) = \{\emptyset, Q, \bar{Q}, Q \cap \bar{Q}, Q \cup \bar{Q}\}$. Assigning a mass to $Q \cap \bar{Q}$ is meaningless, so we only assign a mass to elements in $D(\theta) \setminus Q \cap \bar{Q} = \{\emptyset, Q, \bar{Q}, Q \cup \bar{Q}\} = 2^\theta$ (it is actually Shafer's model [30]).

To compute the belief masses for a given source of information i , we defined a test T_i on the degree of match $dm_i : T_i(x, x_q)$ is true if $dm(x, x_q) \geq \tau_i$, $0 \leq \tau_i \leq 1$, and false otherwise. The mass functions are then assigned according to $T_i(x, x_q)$.

- if $T_i(x, x_q)$ is true:
 - $m_i(Q) = P(T_i(x, x_q)|x \text{ is relevant for } x_q)$ (the sensitivity of T_i)
 - $m_i(Q \cup \bar{Q}) = 1 - m_i(Q)$
 - $m_i(\bar{Q}) = 0$
- else
 - $m_i(\bar{Q}) = P(\overline{T_i(x, x_q)}|x \text{ is not relevant for } x_q)$ (the specificity of T_i)
 - $m_i(Q \cup \bar{Q}) = 1 - m_i(\bar{Q})$
 - $m_i(Q) = 0$.

The sensitivity (resp. the specificity) represents the degree of confidence in a positive (resp. negative) answer to test T_i ; $m_i(Q \cup \bar{Q})$ is assigned the degree of uncertainty. The sensitivity of T_i , for a given threshold τ_i , is defined as the percentage of pairs of training documents (y_1, y_2) from the same class such that $T_i(y_1, y_2)$ is true. Similarly, the specificity of T_i is defined as the percentage of pairs of training documents (z_1, z_2) from different classes such that $T_i(z_1, z_2)$ is false. Test T_i is relevant if it is both sensitive and specific. As τ_i increases, sensitivity increases and specificity decreases. So, we set τ_i as the intersection of the two curves "sensitivity according to τ_i " and "specificity according to τ_i ." A binary search is used to find the optimal τ_i .

D. Retrieval Process

To process a reference document x , every available attribute for x is processed as evidence and Lauritzen and Spiegelhalter's inference algorithm is used to estimate $\alpha_{ij}(x) \forall j, i = 1 \dots M$. If the i th attribute of x_q is available, the degree of match $dm_i(x, x_q)$ is computed according to $\alpha_{ij}(x)$ [see (13)] and the belief masses are computed according to test $T_i(x, x_q)$. The sources available for x_q are then fused. Usual rules of combination have a time complexity exponential in M , which

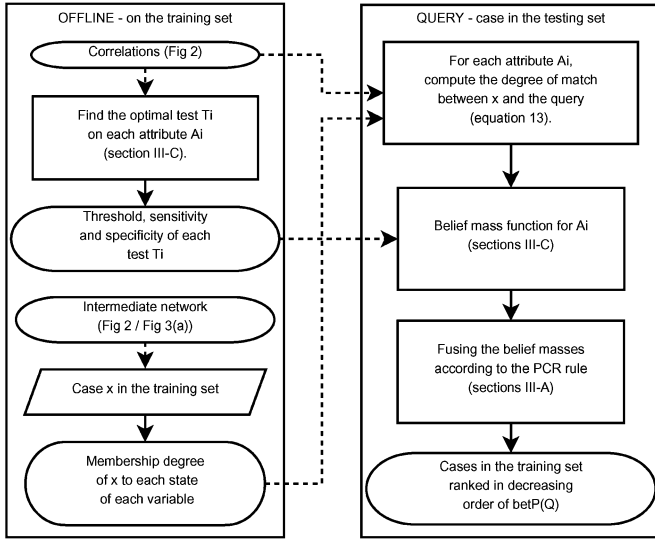


Fig. 5. Bayesian network and Dezert-Smarandache based retrieval.

might be a limitation. So we proposed a rule of combination for two-hypotheses problems (Q and \bar{Q} in our application), adapted from the PCR rules, with a time complexity polynomial in M [34]. Once the sources available for x_q are fused by the proposed rule of combination, the pignistic probability $betP(Q)$ is computed by the following:

$$betP(Q) = m_f(Q) + \frac{m_f(Q \cup \bar{Q})}{2} \quad (16)$$

The process is illustrated in Fig. 4(b) and Fig. 5. The reference documents are then ranked in decreasing order of $betP(Q)$.

IV. APPLICATION TO MEDICAL IMAGE DATABASES

The proposed method has been applied to CADx on two heterogeneous databases. First, it has been applied to diabetic retinopathy severity assessment on a dataset (DRD) built at the Inserm U650 laboratory, in collaboration with ophthalmologists of Brest University Hospital. Then, it has been applied to breast cancer screening on a public access database (DDSM).

A. Diabetic Retinopathy Database

The diabetic retinopathy database contains retinal images of diabetic patients, with associated anonymized information on the pathology. Diabetes is a metabolic disorder characterized by sustained inappropriately high blood sugar levels. This progressively affects blood vessels in many organs, which may lead to serious renal, cardiovascular, cerebral, and also retinal complications. The latter case, namely diabetic retinopathy, can lead to blindness. The database consists of 67 patient files containing 1112 photographs altogether. Images have a definition of 1280 pixels/line for 1008 lines/image. They are lossless compressed images. Patients have been recruited at Brest University Hospital (France) since June 2003 and images were acquired by experts using a Topcon Retinal Digital Camera (TRC-50IA) connected to a computer. An image series is given in Fig. 6.

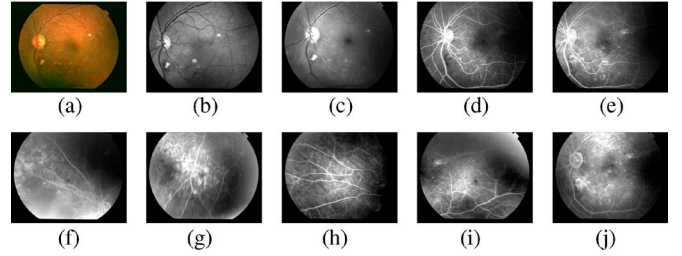


Fig. 6. Photograph sequence of a patient eye. Images (a)–(c) are photographs obtained with different color filters. Images (d)–(j) constitute a temporal angiographic series: a contrast agent (fluorescein) is injected and photographs are taken at different stages [early (d), intermediate (e)–(i), late (j)]. At the intermediate stage, photographs from the periphery of the retina are available.

The contextual information available is the age and sex of the patient, as well as structured medical information (see Table I). Patients records consist of at most 10 images per eye (see Fig. 6) and 13 contextual attributes; 12.1% of these images and 40.5% of these contextual attribute values are missing. The disease severity level, according to ICDRS classification [35], was assessed by a single expert for all 67 patients: because of intra-observer variability, the reference standard is imperfect. The distribution of the disease severity among the above-mentioned 67 patients is given in Table II.

B. Digital Database for Screening Mammography (DDSM)

The DDSM project [36], involving the Massachusetts General Hospital, the University of South Florida and the Sandia National laboratories, has built a mammographic image database for research on breast cancer screening. It consists of 2277 patient files. Each of them includes two images of each breast, associated with patient information (age at time of study, subtlety rating for abnormalities, American College of Radiology breast density rating and keyword description of abnormalities) and image information (scanner, spatial resolution, etc.). The following contextual attributes are used in this study:

- the age at time of study;
- the breast density rating.

Images have a varying definition, of about 2000 pixels/line for 5000 lines/image. An example of image sequence is given in Fig. 7. There is no missing information in DDSM.

Each patient file has been graded by a physician. Patients are then classified in three groups: normal, benign and cancer. The distribution of grades among the patients is given in Table II. The reference standard is also affected by intra- and inter-observer variability in this dataset.

C. Objective of the System

Definition: Let x_q be a query document, and $x_1, x_2, \dots, x_{\mathcal{K}}$ be its \mathcal{K} most similar documents within the training set. The precision at \mathcal{K} for x_q is the fraction of documents, among $\{x_1, x_2, \dots, x_{\mathcal{K}}\}$, that belong to the same class as x_q .

For each query document, we want to retrieve the most similar reference documents in a given database. Satisfaction of the user's needs can thus be assessed by the precision at \mathcal{K} . The average precision at \mathcal{K} measures how good a fusion method is

TABLE I
STRUCTURED CONTEXTUAL INFORMATION FOR DIABETIC RETINOPATHY PATIENTS

category	attributes	possible values
general clinical context	family clinical context	diabetes, glaucoma, blindness, misc.
	medical clinical context	arterial hypertension, dyslipidemia, proteinuria, renal dialysis, allergy, misc.
	surgical clinical context	cardiovascular, pancreas transplant, renal transplant, misc.
	ophthalmologic clinical context	cataract, myopia, AMD, glaucoma, unclear medium, cataract surgery, glaucoma surgery, misc.
examination and diabetes context	diabetes type	none, type I, type II
	diabetes duration	< 1 year, 1 to 5 years, 5 to 10 years, > 10 years
	diabetes stability	good, bad, fast modifications, glycosylated hemoglobin
	treatments	insulin injection, insulin pump, anti-diabetic drug + insulin, anti-diabetic drug, pancreas transplant
eye symptoms reported before the angiography test	ophthalmologically symptomatic	none, systematic ophthalmologic screening - known diabetes, recently diagnosed diabetes by check-up, diabetic diseases other than ophthalmic ones
	ophthalmologically asymptomatic	none, infection, unilateral decreased visual acuity (DVA), bilateral DVA, neovascular glaucoma, intra-retinal hemorrhage, retinal detachment, misc.
maculopathy	maculopathy	focal edema, diffuse edema, none, ischemic

TABLE II
PATIENT DISEASE SEVERITY DISTRIBUTION

database	disease severity	number of patients
DRD	no apparent diabetic retinopathy	7
	mild non-proliferative	9
	moderate non-proliferative	22
	severe non-proliferative	9
	proliferative	9
	treated/non active diabetic retinopathy	11
DDSM	normal	695
	benign	669
	cancer	913

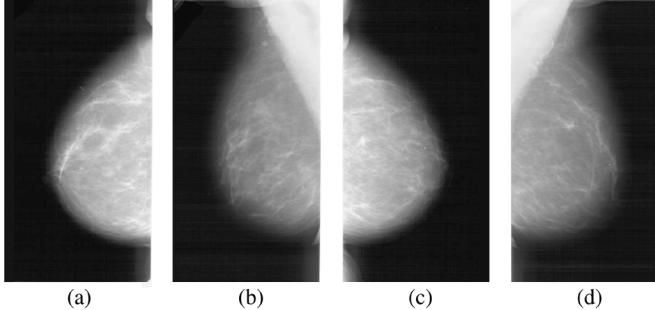


Fig. 7. Mammographic image sequence of the same patient. (a) and (b) Two views of the left breast. (c) and (d) Two views of the right one.

at combining feature-specific distance measures into a semantically meaningful distance measure.

D. Patient File Features

In those databases, each patient file consists of both digital images and contextual information. Contextual attributes (13 in DRD, 2 in DDSM) are processed as-is in the CBR system. Images need to be processed in order to extract relevant digital features. A possible solution is to segment these images and extract domain specific information (such as the number of lesions); for DRD, the number of automatically detected microaneurysms (the most frequent lesion of diabetic retinopathy) [37] is used. However, this kind of approach requires expert knowledge and a robust segmentation of images, which is not always possible because of acquisition variability. So, an additional solution to characterize images by their digital content, without segmenting images, is proposed: a feature vector

is extracted from the wavelet decomposition of the image [25]. An image signature is computed for each image field in a document (4 in DDSM: RCC, RMLO, LCC, LMLO and 10 in DRD); each image signature is associated with an attribute (see Section II-C). In conclusion, there are 24 attributes in DRD and six attributes in DDSM.

E. Training and Test Sets

Retrieval performance is assessed as follows. Both datasets are randomly divided into five subsets V_1, V_2, \dots, V_5 of equal size. Each subset $V_i, i = 1 \dots 5$, is used in turn as test set while the remaining four subsets are used for training the retrieval system. Note that the test set is completely independent from the training process.

F. Results

The number of documents proposed by the system is typically set to $\mathcal{K} \in \{5, 10, 20\}$. Precisions obtained with each fusion method are reported in Table III. Because the cardinality of each class is small in DRD, performance was expected to decrease as \mathcal{K} increases. For both databases, at $\mathcal{K} = 5$, the average precision is greater than 0.8; it means that, on average, more than 80% of the selected documents are relevant for a query. We can see that, on DRD, the use of DSMT increases the average precision at $\mathcal{K} = 5$ by about 10%, but not on DDSM. This can be explained by the fact that, on DRD, many sources of information are contextual: less reliable similarity measures are derived from these contextual sources (the sensitivity/specificity values of the corresponding tests T_i are lower), hence the interest of DSMT for this database. To assess the performance of the proposed fusion framework, independently of the underlying image signatures (described in Section II-C-1), it was compared to an early fusion [6] and a late fusion method [8] based on the same image signatures. The results we obtained for these methods are summarized in Table III.

The average computation time to retrieve the five closest documents for the second method is given in Table IV (computation times are similar with the first method). Clearly, most of the time is spent during the computation of image signatures. All experiments were conducted using an AMD Athlon 64-bit based computer running at 2 GHz.

TABLE III
PRECISION OBTAINED WITH DIFFERENT METHODS

Dataset	DRD			DDSM		
	5	10	20	5	10	20
Bayesian network (see section II)	0.704±0.168	0.654±0.174	0.551±0.191	0.821±0.177	0.813±0.179	0.798±0.191
Bayesian network + DSMT (see section III)	0.809±0.158	0.693±0.165	0.590±0.180	0.803±0.182	0.801±0.185	0.787±0.188
Bayesian network + DSMT (simplified signature computation)	0.806±0.158	0.693±0.165	0.587±0.180	0.800±0.184	0.799±0.186	0.787±0.189
Bayesian network + DSMT (images only)	0.704±0.176	0.640±0.181	0.529±0.200	0.759±0.192	0.740±0.194	0.725±0.194
Early fusion [6]	0.430±0.207	0.448±0.203	0.432±0.212	0.714±0.193	0.731±0.192	0.718±0.196
Late fusion [8]	0.394±0.210	0.431±0.194	0.427±0.204	0.703±0.192	0.717±0.191	0.700±0.200

TABLE IV
COMPUTATION TIMES FOR THE DSMT BASED METHOD

database	DRD	DDSM
retrieval (once signatures are computed)	0.37 s	4.67 s
<i>Do's generalized Gaussian estimation method</i>		
computing the signatures (for 1 image)	4.57 s	35.89 s
average retrieval time (the average number of images per document is ≈ 9 for DRD and 4 for DDSM)	40.58 s	148.27 s
<i>Simplified generalized Gaussian estimation method — see appendix A</i>		
computing the signatures (for 1 image)	0.25 s	2.23 s
average retrieval time	2.58 s	13.59 s

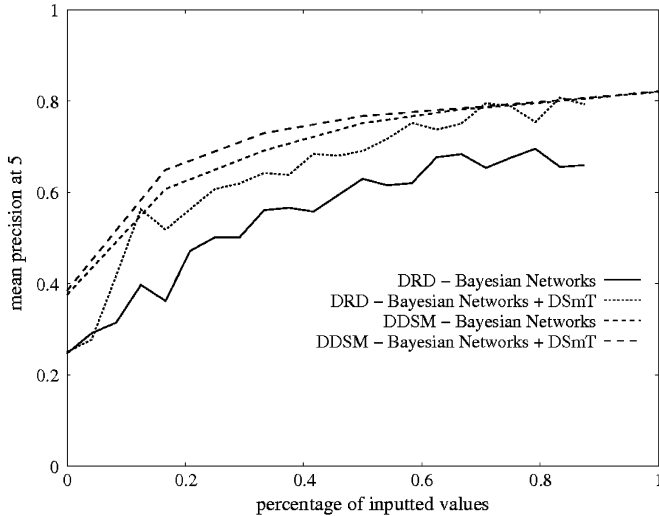


Fig. 8. Robustness with respect to missing values. Note that documents are returned at random when no attributes are available (0 on the x-axis).

To study the robustness of the method with respect to missing values the following test was carried out.

- For each document x_i in the database, 100 new documents were generated as follows. Let n_i be the number of attributes available for x_i , each new example was obtained by removing a number of attribute values randomly selected in $\{0, 1, \dots, n_i\}$.
- The precision at five obtained for these generated documents, with respect to the number of available attributes, was plotted in Fig. 8.

Finally, for comparison purposes, the proposed system was applied to abnormal (“benign” or “cancer”) versus ‘normal’ document classification.

- For each document x_i in the database (1364 abnormal and 695 normal), an abnormality index $a(x_i)$ was defined; $a(x_i)$ is the percentage of abnormal documents among the topmost \mathcal{K} results (if x_i belongs to V_j , then the results are selected within the database minus V_j).

- The receiver-operating curve (ROC) [38] of $a(\cdot)$ was plotted and the area under this curve, noted A_z , was computed.

An area under the ROC curve of $A_z = 0.921$, $A_z = 0.917$ and $A_z = 0.914$ was obtained for $\mathcal{K} = 5$, $\mathcal{K} = 10$ and $\mathcal{K} = 20$, respectively. In comparison, for the task of classifying regions of interest of 512×512 pixels (489 malignant masses, 412 benign masses, and 919 normal breasts), Mazurowski *et al.* obtained an area under the ROC curve of $A_z = 0.907 \pm 0.024$ using mutual information [38].

V. DISCUSSION AND CONCLUSION

In this paper, we introduced two methods to include image series and their signatures, with contextual information, in a CBR system. The first method uses a Bayesian network to model the relationships between attributes. It allows us to manage missing information, and to fuse several sources of information. In particular, a method to include image signatures in a Bayesian network was proposed. In this first method, we modeled the relevance of a reference document in the database for the query, according to a given attribute A_i , through the design of conditional probabilities $P_q(A_i = a_{ij}|Q)$. The second method, based on the Dezert–Smarandache theory, extends the first one by improving the fusion operator: we modeled our confidence in each estimation of the relevance through the design of belief mass functions. These methods have been successfully applied to two medical image databases. These methods are generic: they can be extended to databases containing sound, video, etc. The wavelet transform based signature, presented in Section II-C, can be applied to any n -dimensional digital signal, using its n -dimensional wavelet transform ($n = 1$ for sound, $n = 3$ for video, etc) [39]. Extending the proposed image signature to n -dimensional wavelet transforms is trivial: characterizing the distribution of wavelet coefficients simply implies iterating over rows, columns, depth (or time), etc., instead of rows and columns for a 2-D image (see Appendix A). The proposed methods are also convenient in the sense that they do not need to be retrained each time a new document is included in the database.

The precision at five obtained for DRD (0.809 ± 0.158) is particularly interesting, considering the few examples available, the large number of missing values and the large number of classes taken into account. On this database, the methods outperform usual methods by almost a factor of 2 in terms of precision at 5. The improvement is also noticeable on DDSM (0.821 ± 0.177 compared to 0.714 ± 0.193). The proposed retrieval methods are fast: most of the computation time is spent during the image processing steps. The code may be parallelized to decrease computation times further. Moreover, sufficient precision

can be reached before all the attributes are provided by the user. As a consequence, the user can stop formulating his query when the returned results are satisfactory. On DRD for instance, a precision at five of 0.6 can be reached by providing less than 30% of the attributes (see Fig. 8): with this precision, the majority of the retrieved documents (3 out of 5) belong to the right class. Table III shows that the difference, in terms of retrieval performance, between single image retrieval [25] and heterogeneous document retrieval, comes from the combination of image features extracted from several images, more than the inclusion of contextual attributes.

This study has three limitations. First, only one type of image feature [25] has been included in the retrieval system (two for DRD [25], [37]). In particular, the inclusion of application-specific image features will have to be validated on several medical image databases. Second, the reference standards are affected by inter- and intra- observer variability, further validation and observer studies are needed. Finally, as it has been shown by Cheng *et al.* the size of the dataset has an influence on the correctness of the generated Bayesian networks. DRD, in particular, is small compared to the datasets used to validate Bayesian network generation methods [24]. The limited size of the dataset may also impact the performance on the test set, especially if \mathcal{K} is larger than (or is in the order of) the number of cases belonging to some of the classes within the dataset.

As a conclusion, using appropriate information fusion operators, heterogeneous case retrieval in medical digital databases is a powerful tool to build reliable CADx systems. In future works, we will try to improve retrieval performance further through the use of relevance feedback [4] and through the inclusion of localized image features. A web interface, that will permit relevance feedback, is being developed to allow assessment of clinical usefulness by physicians.

APPENDIX A

FAST PARAMETER ESTIMATION FOR GENERALIZED GAUSSIAN DISTRIBUTIONS

In Do's parameter estimation method [27], the parameters of the wavelet coefficient distribution in a $M \times N$ subband $\mathcal{X} = \{x_{i,j}, i = 1 \dots M, j = 1 \dots N\}$, namely $\hat{\alpha}$ and $\hat{\beta}$, are obtained by iterating over all coefficients in this subband. For instance, $\hat{\alpha}$ is obtained as follows:

$$\hat{\alpha} = \left(\frac{\beta}{MN} \sum_{i=1}^M \sum_{j=1}^N |x_{i,j}|^\beta \right)^{\frac{1}{\beta}} \quad (17)$$

where β is an approximation of $\hat{\beta}$, which is iteratively refined using the Newton–Raphson procedure [27]. The computation of $\hat{\beta}$ relies, for each wavelet coefficient, on multiple evaluations of the logarithm and the digamma function, which implies slow computations.

We propose to significantly reduce the number of such evaluations by applying Do's estimation method, not directly to \mathcal{X} , but to a histogram of \mathcal{X} .

- 1) The standard deviation σ of \mathcal{X} is computed.
- 2) A B -bins histogram of \mathcal{X} , restricted to the $[-n\sigma; n\sigma]$ interval, is computed (we used $B = 64$ and $n = 5$ —these

numbers were chosen to reduce the approximation error on an independent dataset¹).

- 3) Let h_k be the number of coefficients assigned to the k th bin, and v_k the centroid of that bin.

$$v_k = -n\sigma + \left(k - \frac{1}{2} \right) \frac{2n\sigma}{B}. \quad (18)$$

Equation (17) becomes

$$\hat{\alpha} = \left(\frac{\beta}{MN} \sum_{k=1}^B h_k |v_k|^\beta \right)^{\frac{1}{\beta}}. \quad (19)$$

All other equations in [27] are modified similarly.

APPENDIX B

$P_q(A_i = a_{ij}|Q)$: COMPUTATION DETAILS

For each attribute $A_i, i = 1 \dots M$, we want $P_q(Q|A_i = a_{ij})$ to be proportional to $r_{ij} = \sum_{k=1}^M \alpha_{ik}(x_q) S_{ijk}$ (see Section II-E). In that purpose, we first determine $p_i = P_q(Q|A_i = a_{i \arg \max_j(r_{ij})})$. Let $\tilde{r}_{ij} = r_{ij} / \max_k(r_{ik})$. The following constraints have to be satisfied:

$$P_q(Q|A_i = a_{ij}) + P_q(\bar{Q}|A_i = a_{ij}) = 1 \quad (20)$$

$$\sum_j P_q(Q|A_i = a_{ij}) P(A_i = a_{ij}) = P_q(Q) \quad (21)$$

$$\sum_j P_q(\bar{Q}|A_i = a_{ij}) P(A_i = a_{ij}) = P_q(\bar{Q}) \quad (22)$$

where $P_q(Q)$, $P_q(\bar{Q})$, and $P(A_i = a_{ij})$ are prior probabilities. Injecting p_i and \tilde{r}_{ij} in (21), we obtain

$$\sum_j p_i \tilde{r}_{ij} \cdot P(A_i = a_{ij}) = P_q(Q), \quad i = 1 \dots M \quad (23)$$

p_i is then extracted from (23)

$$p_i = \frac{P_q(Q)}{\sum_j \tilde{r}_{ij} \cdot P(A_i = a_{ij})}, \quad i = 1 \dots M. \quad (24)$$

Once p_i is computed, $P_q(\bar{Q}|A_i = a_{i \arg \max_j(r_{ij})}) = 1 - p_i$ can be computed [see (20)]. Other conditional probabilities are deduced from the definition of $\tilde{r}_{ij} : P_q(Q|A_i = a_{ij}) = p_i \cdot \tilde{r}_{ij}$.

If the most desirable state for attribute $A_i(\arg \max_j(r_{ij}))$ is a rare state, it is possible that $p_i > 1$. Indeed, in constraint (21), $P_q(Q|A_i = a_{i \arg \max_k(r_{ik})})$ is multiplied by a small value ($P(A_i = a_{i \arg \max_k(r_{ik})})$), the result of this product is small and the other terms of the sum (with a value $P_q(Q|A_i = a_{ij})$ smaller than $P_q(Q|A_i = a_{i \arg \max_j(r_{ij})})$ by definition) might be too small for the sum to reach $P_q(Q)$. In that case, the conditional probabilities should be changed as follows:

- we set $p_i = 1$,
- each $\tilde{r}_{ij}, j \neq \arg \max_k(r_{ik})$, is multiplied by a constant $\gamma > 0$.

With this setup, constraint (21) becomes

$$P(A_i = a_{ij}) + \sum_{j \neq \arg \max_k(r_{ik})} \gamma \cdot \tilde{r}_{ij} \cdot P(A_i = a_{ij}) = P_q(Q). \quad (25)$$

¹<http://vismod.media.mit.edu/vismod/imagery/VisionTexture/vistex.html>.

Finally, γ is extracted from (26) and conditional probabilities from (27)

$$\gamma = \frac{P_q(Q) - P(A_i = a_{i \arg \max_j(r_{ij})})}{\sum_{j \neq \arg \max_k(r_{ik})} \tilde{r}_{ij} \cdot P(A_i = a_{ij})} \quad (26)$$

$$P_q(Q|A_i = a_{ij}) = \gamma \cdot \tilde{r}_{ij}, \quad j \neq \arg \max_j(r_{ij}). \quad (27)$$

The inequality $P_q(Q) \geq P(A_i = a_{i \arg \max_k(r_{ik})})$ always holds, as a consequence $\gamma > 0$. Indeed $P_q(Q) \geq P_q(Q|A_i = a_{i \arg \max_k(r_{ik})})P(A_i = a_{i \arg \max_k(r_{ik})})$ [according to constraint (21)], i.e., $P_q(Q) \geq p_i \cdot P(A_i = a_{i \arg \max_k(r_{ik})})$; given that $p_i = 1$, the following inequality holds: $P_q(Q) \geq P(A_i = a_{i \arg \max_k(r_{ik})})$.

REFERENCES

- [1] A. Aamodt, "Case-based reasoning: Foundational issues, methodological variations, and system approaches," *AI Commun.*, vol. 7, no. 1, pp. 39–59, 1994.
- [2] I. Bichindaritz and C. Marling, "Case-based reasoning in the health sciences: What's next?," *Artif. Intell. Med.*, vol. 36, no. 2, pp. 127–135, 2006.
- [3] J.-M. Cauvin, C. le Guillou, B. Solaiman, M. Robaszekiewicz, P. le Beux, and C. Roux, "Computer-assisted diagnosis system in digestive endoscopy," *IEEE Trans. Inf. Technol. Biomed.*, vol. 7, no. 4, pp. 256–262, Dec. 2003.
- [4] A. W. M. Smeulders, M. Worring, S. Santini, A. Gupta, and R. Jain, "Content-based image retrieval at the end of the early years," *IEEE Trans. Pattern Anal. Mach. Intell.*, vol. 22, no. 12, pp. 1349–1380, Dec. 2000.
- [5] H. Müller, N. Michoux, D. Bandon, and A. Geissbuhler, "A review of content-based image retrieval systems in medical applications—Clinical benefits and future directions," *Int. J. Med. Inform.*, vol. 73, no. 1, pp. 1–23, 2004.
- [6] D. R. Wilson and T. R. Martinez, "Improved heterogeneous distance functions," *J. Artif. Intell. Res.*, vol. 6, pp. 1–34, 1997.
- [7] R. K. Srihari, A. Rao, B. Han, S. Munirathnam, and X. Wu, "A model for multimodal information retrieval," in *IEEE Int. Conf. Multimedia Expo*, New York City, 2000, pp. 701–704.
- [8] R. Nuray and F. Can, "Automatic ranking of information retrieval systems using data fusion," *Inf. Process. Manag.*, vol. 42, no. 3, pp. 595–614, 2006.
- [9] S. Wu and S. McClean, "Performance prediction of data fusion for information retrieval," *Inf. Process. Manag.*, vol. 42, no. 4, pp. 899–915, 2006.
- [10] H. Shao, W.-C. Cui, and H. Zhao, "Medical image retrieval based on visual contents and text information," in *IEEE Int. Conf. Syst., Man Cybern.*, The Hague, The Netherlands, 2004, pp. 1098–1103.
- [11] Z. Zhang, R. Zhang, and J. Ohya, "Exploiting the cognitive synergy between different media modalities in multimodal information retrieval," in *IEEE Int. Conf. Multimedia Expo*, Taipei, Taiwan, 2004, pp. 2227–2230.
- [12] P. Buitelaar, P. Cimiano, A. Frank, M. Hartung, and S. Racioppa, "Ontology-based information extraction and integration from heterogeneous data sources," *Int. J. Human Comput. Studies*, vol. 66, no. 11, pp. 759–788, 2008.
- [13] S. Antani, L. R. Long, and G. R. Thoma, "A biomedical information system for combined content-based retrieval of spine X-ray images and associated text information," in *Proc. Indian Conf. Comput. Vis., Graphics, Image Process.*, Ahmadabad, India, 2002, pp. 242–247.
- [14] C. le Bozec, E. Zapletal, M. C. Jaulent, D. Heudes, and P. Degoulet, "Towards content-based image retrieval in a HIS-integrated PACS," in *Proc. Annu. Symp. Am. Soc. Med. Informatics*, Los Angeles, CA, 2000, pp. 477–481.
- [15] E. Chaum, T. P. Karnowski, V. P. Govindasamy, M. Abdelrahman, and K. W. Tobin, "Automated diagnosis of retinopathy by content-based image retrieval," *Retina*, vol. 28, no. 10, pp. 1463–1477, 2008.
- [16] E. Bruno, N. Moenne-Loccoz, and S. Marchand-Maillet, "Design of multimodal dissimilarity spaces for retrieval of video documents," *IEEE Trans. Pattern Anal. Mach. Intell.*, vol. 30, no. 9, pp. 1520–1533, Sep. 2008.
- [17] F. Smarandache and J. Dezert, *Advances and Applications of DSMT for Information Fusion I*. Rehoboth, NM: American Research Press, 2004 [Online]. Available: <http://fs.gallup.unm.edu/DSMT-book1.pdf>
- [18] H. Turtle, "Inference networks for document retrieval," Ph.D. dissertation, Univ. Massachusetts, 1991.
- [19] M. Indrawan, "A framework for information retrieval based on Bayesian networks," Ph.D. dissertation, Monash Univ., Victoria, Australia, 1998.
- [20] C. Wilson, B. Srinivasan, and M. Indrawan, "A general inference network based architecture for multimedia information retrieval," in *IEEE Int. Conf. Multimedia Expo*, New York, 2000, pp. 347–350.
- [21] H. Ghosh, P. Poornachander, A. Mallik, and S. Chaudhury, "Learning ontology for personalized video retrieval," in *Int. Multimedia Conf.*, Augsburg, Germany, 2007, pp. 39–46.
- [22] J. Pearl, *Probabilistic Reasoning in Intelligent Systems: Networks of Plausible Inference*. San Francisco, CA: Morgan Kaufmann, 1988.
- [23] S. L. Lauritzen and D. J. Spiegelhalter, "Local computations with probabilities on graphical structures and their application to expert systems," *J. R. Stat. Soc.*, vol. 50, no. 2, pp. 157–224, 1988.
- [24] J. Cheng, R. Greiner, J. Kelly, D. Bell, and W. Liu, "Learning Bayesian networks from data: An information-theory based approach," *Artif. Intell.*, vol. 137, no. 1, pp. 43–90, 2002.
- [25] G. Quellec, M. Lamard, G. Cazuguel, B. Cochener, and C. Roux, "Wavelet optimization for content-based image retrieval in medical databases," *Med. Image Anal.*, vol. 14, no. 2, pp. 227–241, 2010.
- [26] G. van de Wouwer, P. Scheunders, and D. van Dyck, "Statistical texture characterization from discrete wavelet representations," *IEEE Trans. Image Process.*, vol. 8, no. 4, pp. 592–598, Apr. 1999.
- [27] M. N. Do and M. Vetterli, "Wavelet-based texture retrieval using generalized Gaussian density and Kullback-Leibler distance," *IEEE Trans. Image Process.*, vol. 11, no. 2, pp. 146–158, Feb. 2002.
- [28] J. C. Bezdek, "Fuzzy mathematics in pattern classification," Ph.D. dissertation, Cornell Univ., New York, 1973.
- [29] A. Strehl, "Relationship-based clustering and cluster ensembles for high-dimensional data mining," Ph.D. dissertation, Univ. Texas, Austin, 2002.
- [30] G. Shafer, *A Mathematical Theory of Evidence*. Princeton, NJ: Princeton Univ. Press, 1976.
- [31] F. Smarandache and J. Dezert, *Advances and Applications of DSMT for Information Fusion II*. Rehoboth, NM: American Research Press, 2006 [Online]. Available: <http://fs.gallup.unm.edu/DSMT-book2.pdf>
- [32] P. Smets, "Constructing the pignistic probability function in a context of uncertainty," in *Proc. 5th Annu. Conf. Uncertainty Artif. Intell.*, North-Holland, The Netherlands, 1990, pp. 29–40.
- [33] J. Dezert and F. Smarandache, *An Introduction to DSMT French Aerospace Research Lab.*, Univ. New Mexico, Albuquerque, Tech. Rep., 2009 [Online]. Available: <http://fs.gallup.unm.edu/Introduction-ToDSMT.pdf>
- [34] G. Quellec, "Indexation et fusion multimodale pour la recherche d'information par le contenu. application aux bases de données d'images médicales," Ph.D. dissertation, Bretagne, France, 2008.
- [35] C. Wilkinson, F. Ferris, and R. Klein *et al.*, "Proposed international clinical diabetic retinopathy and diabetic macular edema disease severity scales," *Ophthalmology*, vol. 110, no. 9, pp. 1677–1682, 2003.
- [36] M. Heath, K. Bowyer, D. Kopans, R. Moore, and W. P. Kegelmeyer, "The digital database for screening mammography," in *Proc. 5th Int. Workshop Digital Mammogr.*, Toronto, ON, Canada, 2000, pp. 212–218.
- [37] G. Quellec, M. Lamard, P. M. Josselin, G. Cazuguel, B. Cochener, and C. Roux, "Optimal wavelet transform for the detection of microaneurysms in retina photographs," *IEEE Trans. Med. Imag.*, vol. 27, no. 9, pp. 1230–1241, Sep. 2008.
- [38] M. A. Mazurowski, P. A. Habas, J. M. Zurada, and G. D. Tourassi, "Decision optimization of case-based computer-aided decision systems using genetic algorithms with application to mammography," *Phys. Med. Biol.*, vol. 53, no. 4, pp. 895–908, Feb. 2008.
- [39] G. Quellec, M. Lamard, G. Cazuguel, B. Cochener, and C. Roux, "Adaptive nonseparable wavelet transform via lifting and its application to content-based image retrieval," *IEEE Trans. Image Process.*, vol. 19, no. 1, pp. 25–35, Jan. 2010.